


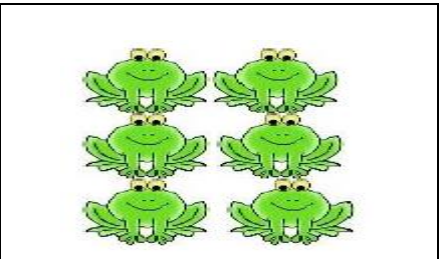

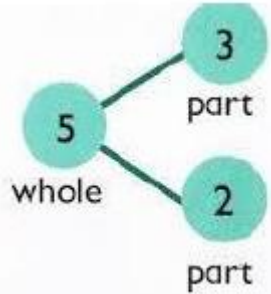

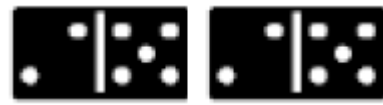



Perran-ar-worthal School Calculation Policy (updated Feb 2020)

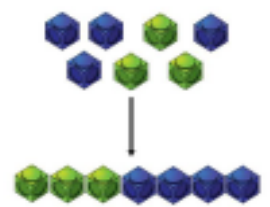
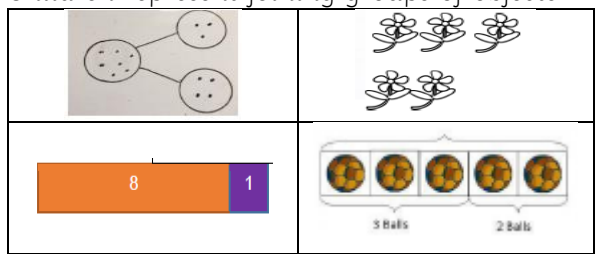
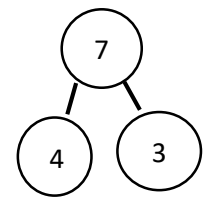
(adapted from the White Rose Calculation Policy)

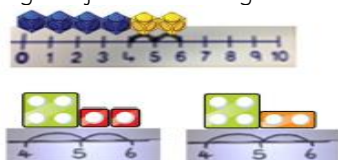
Addition Guidance: <i>Children are always encouraged to think about what is the most efficient method for the calculation</i>	
Stage	
EYFS Statutory Requirements 2014	<p>Pupils should be taught to:</p> <ul style="list-style-type: none"> <li>• Birth –to 11 months – notice changes in number of objects / images, sounds in groups of and up to 3</li> <li>• 8 – 20 months - has some understanding that things exist even when out of sight</li> <li>• 16-26 months – Begins to organise and categorise objects -sorting</li> <li>• 22 – 36 months – knows that a group of things changes in quantity when something is added or taken away</li> <li>• 30 – 50 – separates a group of 3 or 4 objects in different ways beginning to recognise that the total is still the same</li> <li>• 40-60 – finds the total number of items in two groups by counting all of them</li> </ul> <p>In practical activities and discussions begin to use the vocabulary involved in addition</p>
EYFS  1	<p>Counting objects, counting songs, sorting objects, recognising numbers in the inside and outside environment, counting and numbers in stories and poems and counting along number lines.</p> <div style="display: flex; justify-content: space-around;">     </div>
EYFS  2	<p>Pupils should be taught to:</p> <p>Early Learning Goal - Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer.</p> <p>Count on from first group to add two groups of objects.</p>

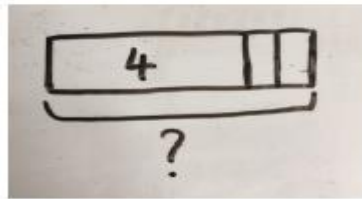
 <p><math>5 + ? = 10</math></p> 	<div style="border: 1px solid black; padding: 5px;">  <p>Put biggest number in your head and count on using fingers or objects</p> </div> 	 <p>Progression <math>6 + 3 = 9</math></p> <p>Use unifix</p> <p>Use unifix on number track</p> <p>Use number track without unifix</p> <p>Use numberline</p> <p>Numicon</p>
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Year 1 Stages 2/3/4/5	Year 2 Stages 5/6/7	Year 3 Stages 7/8 (Up to 3 digits)	Year 4 Stages 8/9 (Up to 4 digits)	Year 5 Stage 9 (Up to 6 digits and decimals)	Year 6 Stage 9 (Up to 7 digits and decimals)
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Stages	Concrete	Pictorial	Abstract
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3	<p>Combining two parts to make a whole (using a variety of objects)</p> 	<p>Children represent joining groups of objects</p> 	<p>4 is a part. 3 is a part. 7 is a whole.</p> <p><math>4 + 3 = 7</math></p> 
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4	<p>Counting on from the largest number</p> 	<p>A bar model which encourages the children to count on, rather than count all.</p>	<p>Use an abstract number line:</p> <ul style="list-style-type: none"> <li>• What is 2 more than 4?</li> <li>• What is the sum of 2 and 4?</li> <li>• What is the total of 4 and 2?</li> <li>• <math>4 + 2</math></li> </ul>
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5

Regrouping to make 10, using ten frames and counters/cubes or using Numicon.

$6 + 5$

Children to draw the ten frame and counters / cubes.

Children to develop an understanding of equality:

$6 + \square = 11$

$6 + 5 = 5 + \square$

$6 + 5 = \square + 4$

6

Adding 3 objects  
 $4 + 7 + 6 = 17$   
 Put 4 and 6 together to make 10. Add on 7

Draw pictures to recombine groups to make 10:

Combine the 2 numbers that make 10 and then add on the remainder:

$(4 + 7 + 6) = 10 + 7$   
 $= 17$

7

TO + O using base 10. Continue to develop understanding of partitioning and place value.

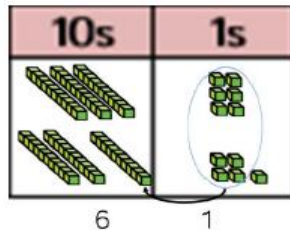
$41 + 8$

Children to represent the base 10 E.g. lines for tens and dots/crosses for ones:

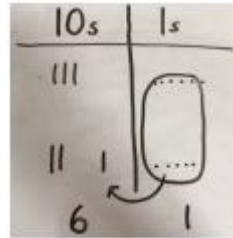
$41 + 8$

8

TO + TO using base 10. Continue to develop understanding of partitioning and place value:  $36 + 25$



Children to represent the base 10 in a place value chart:



Looking for ways to make 10

$$36 + 25 =$$

$$\begin{array}{r} 30 + 20 = 50 \\ 5 + 5 = 10 \\ 50 + 10 + 1 = 61 \end{array}$$

36

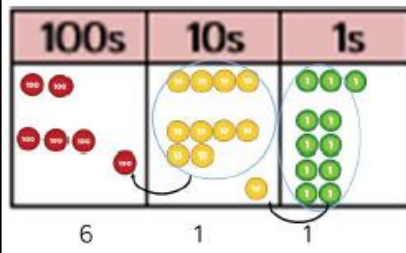
Formal method:

$$\begin{array}{r} +25 \\ 36 \\ \hline 61 \end{array}$$

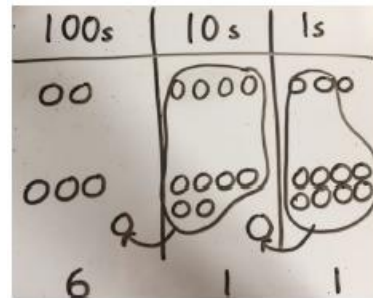
Use rounding to approximate answers.

9

Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column – we exchange for 1 ten, when there are 10 tens in the 10s column – we exchange for 1 hundred:



Children to represent the counters in a place value chart, circling when they make an exchange:




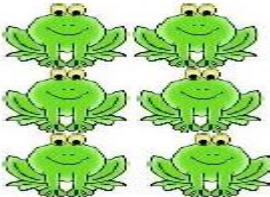
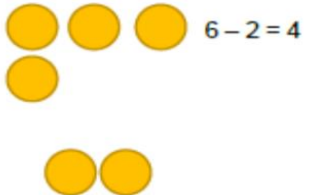
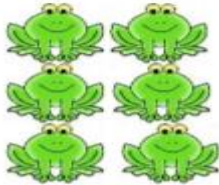


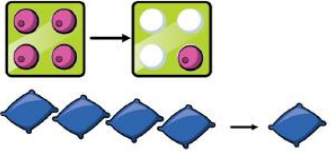
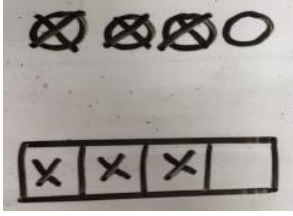
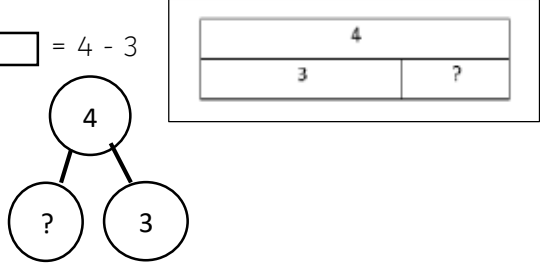

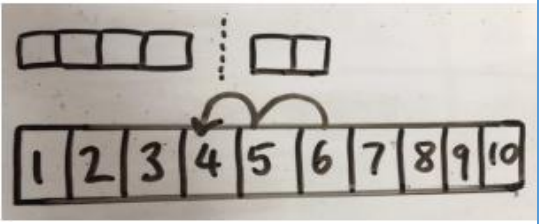
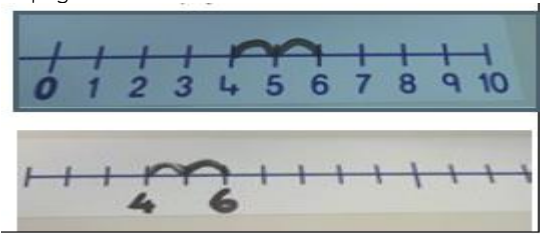
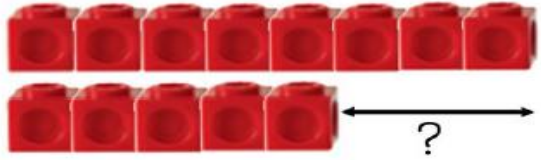
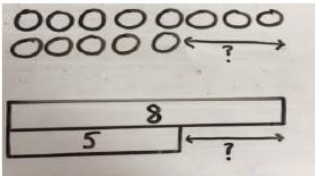
$$\begin{array}{r} 243 \\ +368 \\ \hline 611 \end{array}$$

2	3	.	3	6	1
	9	.	0	8	0
	5	9	.	7	7
	+	1	.	3	0
	9	3	.	5	1
	2	1	.	2	

Use rounding to approximate answers.

Subtraction Guidance: Children are always encouraged to think about what is the most efficient method for the calculation

Stage			
EYFS Statutory Requirement s 2014	<p>Pupils should be taught to:</p> <ul style="list-style-type: none"> <li>• Birth –to 11 months – notice changes in number of objects / images, sounds in groups of and up to 3</li> <li>• 8 – 20 months - has some understanding that things exist even when out of sight</li> <li>• 16-26 months – begins to organise and categorise objects -sorting</li> <li>• 22 – 36 months – knows that a group of things changes in quantity when something is added or taken away</li> <li>• 30 – 50 – separates a group of 3 or 4 objects in different ways beginning to recognise that the total is still the same</li> <li>• 40-60 – understands subtraction as taking away objects from a group and counting on how many are left. In practical activities and discussions begins to use the vocabulary involved in addition and subtraction</li> </ul>		
EYFS  1	<p>Counting objects, counting songs, sorting objects, recognising numbers in the inside and outside environment, counting and numbers in stories and poems and counting along number lines.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div data-bbox="302 686 728 941" style="border: 1px solid black; padding: 5px;">  </div> <div data-bbox="734 686 1164 941" style="border: 1px solid black; padding: 5px;">  </div> <div data-bbox="1171 686 1668 941" style="border: 1px solid black; padding: 5px;">  </div> <div data-bbox="1675 686 2116 941" style="border: 1px solid black; padding: 5px;">  </div> </div>		
EYFS  2	<p>Pupils should be taught to: Early Learning Goal - Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. Count back from large group as you take away - say count back as you take away.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div data-bbox="582 1181 952 1428" style="border: 1px solid black; padding: 10px; text-align: center;"> <math display="block">6 - 2 = 4</math> </div> <div data-bbox="958 1181 1400 1428" style="border: 1px solid black; padding: 10px;">  </div> <div data-bbox="1406 1181 1848 1428" style="border: 1px solid black; padding: 10px;">  </div> </div>		

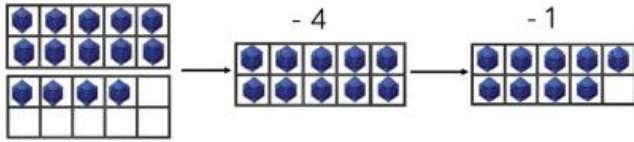
	Year 1 Stages 2/3/4/5	Year 2 Stages 5/6	Year 3 Stages 6/7/8 (Up to 3 digits)	Year 4 Stages 8/9 (Up to 4 digits)	Year 5 Stage 9 (Up to 6 digits and decimals)	Year 6 Stage 9 (Up to 7 digits and decimals)
Stages	Concrete		Pictorial		Abstract	
3	<p>Physically taking away and removing objects from a whole (tens frames, Numicon, cubes etc)</p> <p><math>4 - 3 = 1</math></p> 		<p>Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p> 	<p><math>4 - 3 =</math></p> <p><math>\square = 4 - 3</math></p> 		
4	<p>Counting back (using number lines or number tracks) children start with 6 and count back 2.</p> <p><math>6 - 2 = 4</math></p> 	<p>Children to represent what they see pictorially:</p> 	<p>Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line.</p> 			
5	<p>Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used).</p> <p>Calculate the difference between 8 and 5.</p> 	<p>Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.</p> 	<p>Find the difference between 8 and 5:</p> <p><math>8 - 5</math> the difference is <input type="text"/></p> <p>Children to explore why</p> <p><math>9 - 6 = 8 - 5 = 7 - 4</math> have the same difference</p>			



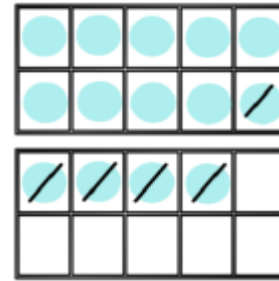
6

Making 10 using ten frames.

$$14 - 5$$



Children to present the ten frame pictorially and discuss what they did to make 10:



Children to show how they can make 10 by partitioning the subtraction:

$$14 - 5 = 9$$

$$\begin{array}{c} 14 - 5 = 9 \\ \swarrow \quad \searrow \\ 4 \quad \quad 1 \end{array}$$

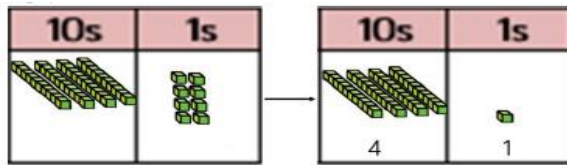
$$14 - 4 = 10$$

$$10 - 1 = 9$$

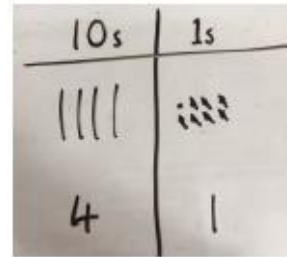
7

Column method using base 10.

$$48 - 7$$

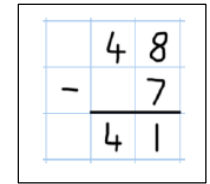


Children to represent the base 10 pictorially:



Column method or children could count back 7.

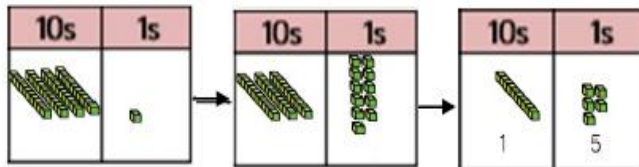
$$48 - 7$$



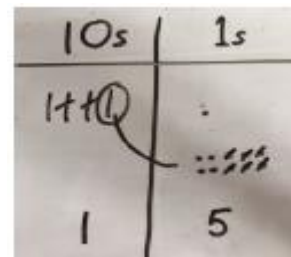
8

Column method using base 10 and having to exchange.

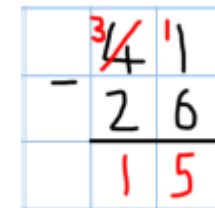
$$41 - 26$$



Represent the base 10 pictorially, remembering to show the exchange:



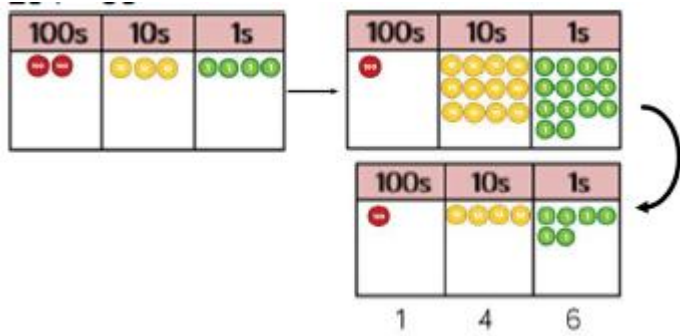
Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because  $41 = 30 + 11$



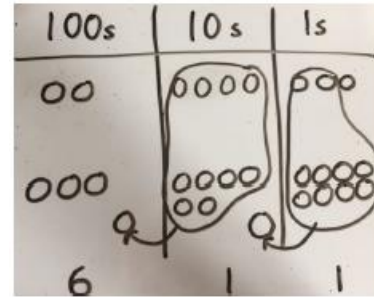
Use rounding to approximate answers.

9

Column method using place value counters.  
234 - 88



Represent the place value counters pictorially, remembering to show what has been exchanged:





Formal column method. Children must understand what has happened when they have crossed out digits:

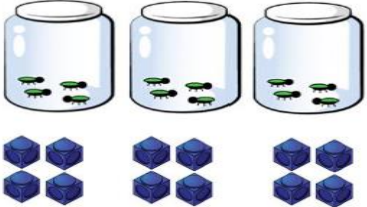
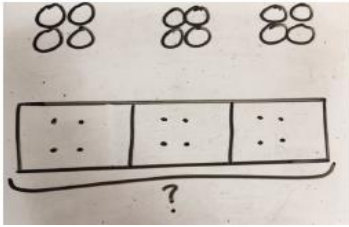
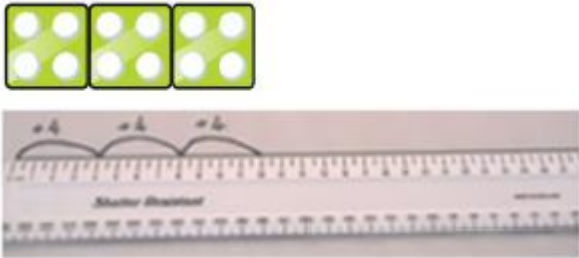
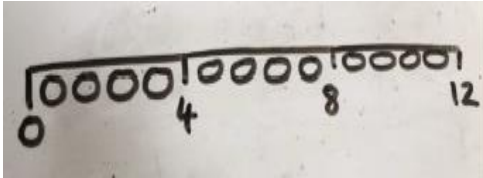
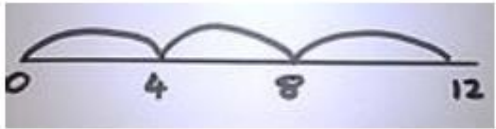
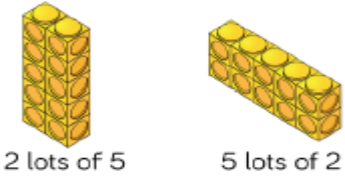
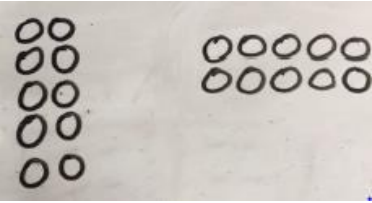
$\begin{array}{r} 234 \\ - 88 \\ \hline 6 \end{array}$	$\begin{array}{r} \text{£}213.83 - \text{£}183.51 \\ \hline \text{H T U} \cdot \text{t h} \\ \cancel{2} \quad \cancel{1} \quad 3 \cdot 8 \quad 3 \\ 1 \quad 8 \quad 3 \cdot 5 \quad 1 \\ \hline 0 \quad 3 \quad 0 \cdot 3 \quad 2 \end{array}$
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Use rounding to approximate answers:



Multiplication Guidance: Children are always encouraged to think about what is the most efficient method for the calculation

Stage						
EYFS Statutory Requirement s 2014						
EYFS  1	N/A					
EYFS  2	<p>Pupils should be taught to: Early Learning Goal Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. They solve problems, including <u>doubling</u>, halving and sharing.</p> <div data-bbox="584 772 1850 995" style="border: 1px solid black; padding: 10px; margin: 10px auto; width: fit-content;"> <div style="display: flex; justify-content: space-between; align-items: center;"> <div style="border-right: 1px solid black; padding-right: 10px;"> <p style="text-align: center; font-weight: bold;">Doubling Songs and Objects</p> </div> <div style="text-align: center;">  </div> <div style="padding-left: 10px;"> <p>Draw pictures to show how to double a number: <b>Double 4 is 8</b></p>  </div> </div> </div>					
	Year 1 Stages 2/3	Year 2 Stages 3/4/5	Year 3 Stages 5/6/7 (Multiply a 2 digit number by a single digit)	Year 4 Stages 7/8 (Multiply a 3 digit number by a single digit)	Year 5 Stage 8 (Multiply 2 digit numbers by 2 and 3 digit numbers)	Year 6 Stage 8 (Multiply any 2 whole or decimal numbers together)

Stages	Concrete	Pictorial	Abstract
3	<p>Repeated grouping/repeated addition  <math>3 \times 4</math>  <math>4 + 4 + 4</math>            There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p> 	<p><math>3 \times 4 = 12</math>  <math>4 + 4 + 4 = 12</math></p>
4	<p>Number lines to show repeated groups:  <math>3 \times 4 =</math></p>  <p>Cuisenaire rods can be used too.</p>	<p>Represent this pictorially alongside a number line E.g:</p> 	<p>Abstract number line showing three jumps of four.</p> <p><math>3 \times 4 = 12</math></p> 
5	<p>Use arrays to illustrate commutativity counters and other objects can also be used:  <math>2 \times 5 = 5 \times 2</math></p> 	<p>Children to represent the arrays pictorially:</p> 	<p>Children to be able to use an array to write a range of calculations E.g.</p> <p><math>10 = 2 \times 5</math>  <math>5 \times 2 = 10</math>  <math>2 + 2 + 2 + 2 + 2 = 10</math>  <math>10 = 5 + 5</math></p>

Partition to multiply using Numicon, base 10 or Cuisenaire rods.

$4 \times 15$

Children to represent the concrete manipulatives pictorially:

Children to be encouraged to show the steps they have taken:

$$\begin{array}{r}
 4 \times 15 \\
 \swarrow \searrow \\
 10 \quad 5 \\
 10 \times 4 = 40 \\
 5 \times 4 = 20 \\
 40 + 20 = 60
 \end{array}$$

Formal column method with place value counters (base 10 can also be used)  $3 \times 23$

Children to represent the counters pictorially:

Children to record what it is they are doing to show understanding

$$\begin{array}{r}
 3 \times 23 \\
 \swarrow \searrow \\
 20 \quad 3 \\
 3 \times 20 = 60 \\
 3 \times 3 = 9 \\
 60 + 9 = 69
 \end{array}$$

Formal column method with place value counters.  $6 \times 23$







Children to represent the counters/base 10, pictorially:

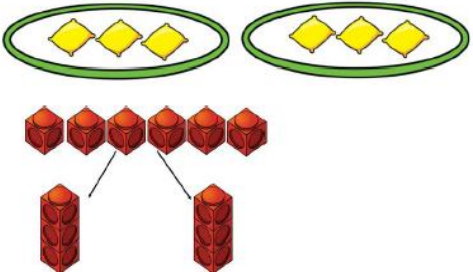
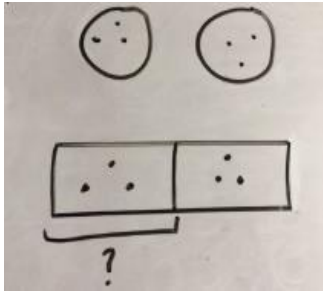

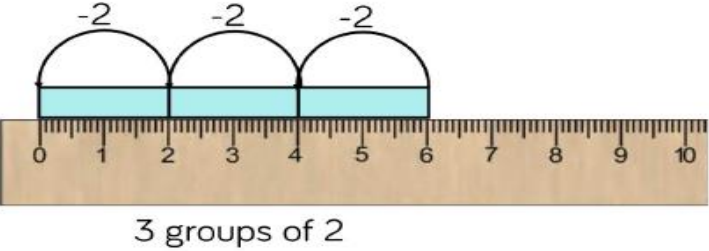
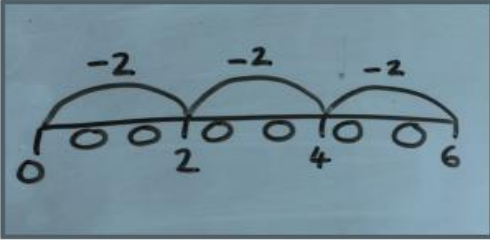
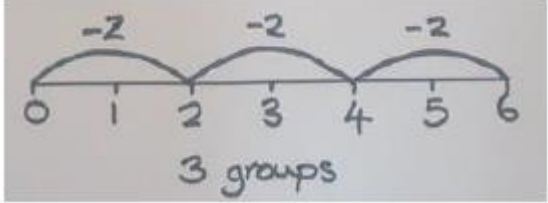

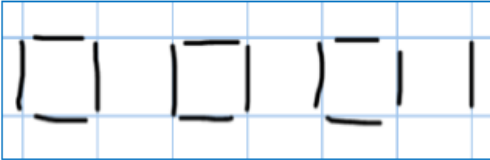

Formal written method:

$  \begin{array}{r}  6 \times 23 = \\  23 \\  \times 6 \\  \hline  138 \\  11  \end{array}  $	$  \begin{array}{r}  124 \\  \times 26 \\  \hline  744 \\  2480 \\  \hline  3224 \\  11  \end{array}  $
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Use rounding to approximate answers.

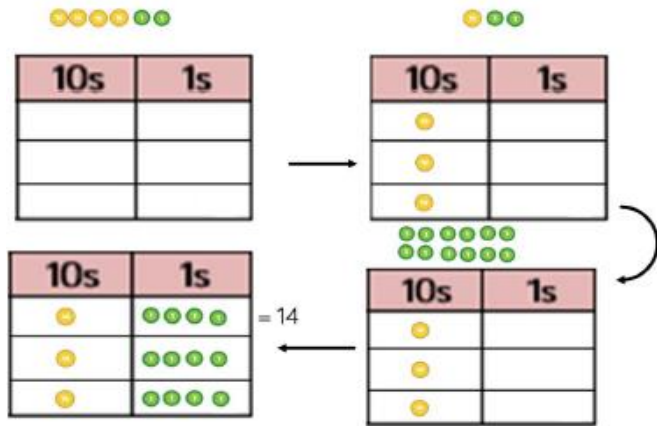
Division Guidance: Children are always encouraged to think about what is the most efficient method for the calculation

Stage								
EYFS Statutory Requirements 2014								
EYFS  1	N/A							
EYFS  2	<p>Pupils should be taught to: Early Learning Goal Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. They solve problems, including doubling, <u>halving</u> and sharing.</p> <table border="1" data-bbox="412 778 1917 1131"> <tr> <td data-bbox="412 778 1258 1131"> <p>Cutting a variety of objects in half:</p>  </td> <td data-bbox="1258 778 1917 1131"> <p>Sharing objects:</p>  </td> </tr> </table>						<p>Cutting a variety of objects in half:</p> 	<p>Sharing objects:</p> 
<p>Cutting a variety of objects in half:</p> 	<p>Sharing objects:</p> 							
Year 1 Stages 2/3	Year 2 Stages 2/3/4	Year 3 Stages 4/5/6 (Divide a 2 digit number by a single digit)	Year 4 Stages 6/7 (Divide a 3 digit number by a single digit)	Year 5 Stage 7/8 (Use short division to divide 4 and 5 digit numbers leaving remainders as decimals and fractions)	Year 6 Stage 8 (Use long division to divide whole and decimal numbers by a 2 digit number)			

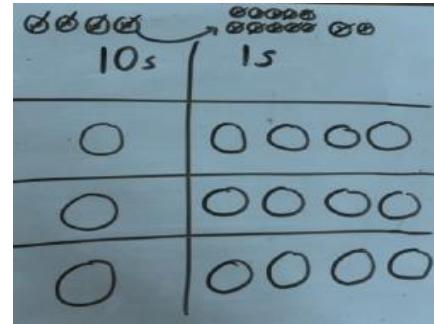
Stages	Concrete	Pictorial	Abstract
3	<p>Sharing using a range of objects.  <math>6 \div 2</math></p> 	<p>Represent the sharing pictorially.</p> 	<p><math>6 \div 2 = 3</math></p>  <p>Children should also be encouraged to use their 2 times tables facts.</p>
4	<p>Repeated subtraction using Cuisenaire rods above a ruler. <math>6 \div 2</math></p>  <p>3 groups of 2</p>	<p>Children to represent repeated subtraction pictorially.</p> 	<p>Abstract number line to represent the equal groups that have been subtracted.</p>  <p>3 groups</p>
5	<p>2 digits <math>\div</math> 1-digit with remainders using a variety of materials. E.g. lollipop sticks, counters and Cuisenaire rods etc.  <math>13 \div 4</math>            Use of lollipop sticks to form wholes- squares are made because we are dividing by 4:</p>  <p>There are 3 whole squares, with 1 left over.</p>	<p>Children to represent the lollipop sticks or lots of pictorially:</p>  <p>There are 3 whole squares, with 1 left over.</p>	<p><math>13 \div 4 = 3</math> remainder 1</p> <p>Children should be encouraged to use their times tables facts; they could also represent repeated addition on a number line.            '3 groups of 4, with 1 left over'</p> 

6

Sharing using place value counters.  
 $42 \div 3 = 14$



Children to represent the place value counters pictorially:



Children to be able to make sense of the place value counters and write calculations to show the process.

$$42 \div 3$$

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

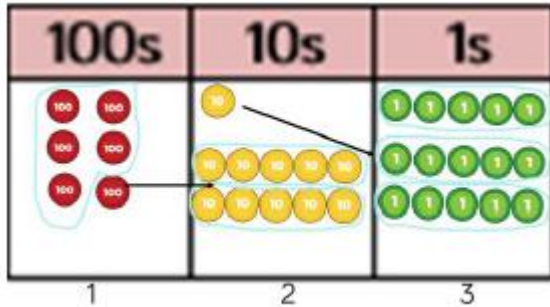
$$12 \div 3 = 4$$

$$10 + 4 = 14$$

Introduce the bus stop method dividing 2 digit numbers by a single digit.

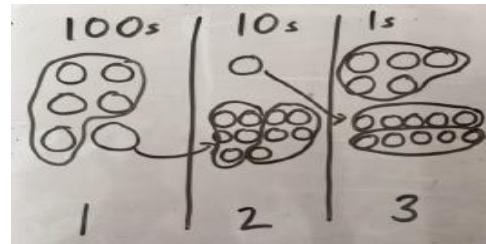
7

Short division using place value counters to group.  
 $615 \div 5$



1. Make 615 with place value counters.
2. How many groups of 5 hundreds can you make with 6 hundred counters?
3. Exchange 1 hundred for 10 tens.
4. How many groups of 5 tens can you make with 11 ten counters?
5. Exchange 1 ten for 10 ones.
6. How many groups of 5 ones can you make with 15 ones?

Represent the place value counters pictorially:



Children to complete the calculation using the short division method (bus stop).

$$\begin{array}{r}
 123 \\
 5 \overline{) 615} \\
 \underline{5 \phantom{00}} \\
 11 \phantom{0} \\
 \underline{10 \phantom{0}} \\
 15 \\
 \underline{15} \\
 0
 \end{array}$$



8

$$1176 \div 6$$

$$\begin{array}{r} 196 \text{ r } 3 \\ 6 \overline{) 115739} \end{array}$$

The remainder is then interpreted as a fraction  $\frac{3}{5}$  and as a decimal:

$$\begin{array}{r} 196.5 \\ 6 \overline{) 115739.30} \end{array}$$

$$432 \div 15$$

$$\begin{array}{r} 28.8 \\ 15 \overline{) 432.0} \\ \underline{30} \phantom{0} \\ 132 \phantom{0} \\ \underline{120} \phantom{0} \\ 120 \phantom{0} \\ \underline{120} \\ 0 \end{array}$$